

# Prediction of unmeasured mode shapes and structural damage detection using least squares support vector machine

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**Abstract.** In this paper, a novel and effective damage diagnosis algorithm is proposed to detect and estimate damage using two stages least squares support vector machine (LS-SVM) and limited number of attached sensors on structures. In the first stage, LS-SVM1 is used to predict the unmeasured mode shapes data based on limited measured modal data and in the second stage, LS-SVM2 is used to predicting the damage location and severity using the complete modal data from the first-stage LS-SVM1. The presented methods are applied to a three story irregular frame and cantilever plate. To investigate the noise effects and modeling errors, two uncertainty levels have been considered. Moreover, the performance of the proposed methods has been verified through using experimental modal data of a mass-stiffness system. The obtained damage identification results show the suitable performance of the proposed damage identification method for structures in spite of different uncertainty levels.

**Keywords:** unmeasured mode shapes; two stages method; LS-SVM; sparse sensors; uncertainty levels

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## 1. Introduction

Damage detection and estimation in engineering structures during their service life has received increasing attention in the last few decades. One of the many nondestructive evaluation methods is based on the change of vibration parameters with a change in the structural properties (Carden and Fanning 2004, Fan and Qiao 2011).

As the number of sensors used to measure modal data is normally limited and usually are less than the number of DOFs in the finite element model, either the model reduction method should be used to match with incomplete measured mode shapes or the measured mode shapes must be expanded to the dimension of the analytical mode shapes (Kourehli *et al.* 2012). Therefore, it is essential to develop algorithms for damage diagnosis using modal data obtained by a limited number of sensors, which means using an incomplete set of modal data (Hosseinzadeh *et al.* 2014). Some researchers used the mode shape expansion methods for structural damage detection (Chen and Bicanic 2000, Au *et al.* 2003) in which others used the model reduction methods (Kourehli *et al.* 2013, Li *et al.* 2008, Kourehli 2015, Rasouli *et al.* 2014). Also, Goh *et al.* (2013) presented an approach combines a two-stage ANN model and statistical method to detect damage based on the limited number of sensors with consideration of uncertainties.

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